

Name: _____
Block: _____

Practice

Algebra 2/Trig H

Collection of problems as practice for the final

(Practice)

Remember:

1. The final-test has only 30 questions. Some with multiple parts.
2. You should SHOW YOUR WORK for all parts of the answer to receive full credit.
3. Clearly indicate (underline/ box/highlight) your final answer. Only ONE answer per question will be considered.

The use of calculator is NOT allowed.

Good luck!!
Dr. Baharav

8. Simplify and give restricted values:

$$\frac{1}{x-4} - \frac{x-1}{x+4} - \frac{6x-16}{x^2-16}$$

$$\begin{aligned} & \frac{(x+4) - x^2 + 5x - 4 - 6x + 16}{(x-4)(x+4)} = \\ & = \frac{-x^2 + 16}{(x-4)(x+4)} = \boxed{-1} \end{aligned}$$

$$\frac{x+4-x^2+5x-4-6x+16}{x^2-16} = -1$$

10. Solve:

$$\frac{2}{x^2-9} - \frac{2}{x+3} = \frac{x-4}{x-3}$$

$$\begin{aligned} & \frac{2}{x^2-9} - \frac{2}{x+3} - \frac{x-4}{x-3} = 0 \\ & \frac{2-2x+6-x^2+x+12}{(x+3)(x-3)} = 0 \\ & 2-2x+6-x^2+x+12 = 0 \\ & x^2+x-20=0 \\ & x = -5 \text{ or } x = 4 \quad \boxed{x=-5 \text{ or } x=4} \end{aligned}$$

12. Solve:

$$\frac{7}{5x-1} = \frac{1}{(x+1)}$$

$$7x+7 = 5x-1$$

$$\begin{aligned} 2x &= -8 \\ x &= -4 \end{aligned}$$

$$\text{Check: } \frac{7}{21} = \frac{1}{-3} \quad \checkmark$$

$$\begin{aligned} x &= 9 \quad \frac{7}{7} - \frac{2}{7} = \frac{4}{1} \\ & 0 = 0 \quad \checkmark \end{aligned}$$

9. Simplify:

$$\frac{1}{x-4} - \frac{x-1}{x^2-x-12}$$

$$\frac{x+3-x+1}{(x-4)(x+3)} = \boxed{\frac{4}{(x-4)(x+3)}}$$

$$\frac{x+3-x+1}{(x-4)(x+3)} = \frac{4}{(x-4)(x+3)}$$

11. Solve:

$$\frac{2}{x^2-3x-4} = \frac{1}{x^2-5x+4}$$

$$\begin{aligned} \frac{2}{(x-4)(x+1)} &= \frac{1}{(x-4)(x-1)} \\ 2(x-1) &= (x+1) \quad \text{check:} \\ \boxed{x=3} \quad \frac{2}{9-9-4} &= \frac{1}{9-15+4} \\ 2(x-1) &= x+1 \implies x=3 \\ -\frac{1}{2} &= -\frac{1}{2} \quad \checkmark \end{aligned}$$

13. Divide using synthetic division:

$$(x^5 + 5x^4 - x^3 - 3x^2 + 5x - 25) \div (x + 5)$$

$$\begin{array}{r} -5 \\ \hline 1 & 5 & -1 & -3 & 5 & -25 \\ & 5 & 0 & 5 & -10 & 25 \\ \hline & 0 & -1 & 2 & -5 & | 0 \\ \hline & & & & & | x^4 - x^2 + 2x - 5 \end{array}$$

$$x^4 - x^2 + 2x - 5$$

$$\begin{aligned} x &= -5: \quad \frac{2}{16} - \frac{2}{-2} = \frac{-4}{-8} \\ & \frac{1}{8} + 1 = \frac{9}{8} \quad \checkmark \end{aligned}$$

14. Divide

$$\frac{30x^8 - 15x^6 + 40x^4}{5x^4}$$

$$\boxed{6x^4 - 3x^2 + 8}$$

$$6x^4 - 3x^2 + 8$$

16. Divide using synthetic division:

$$(x^5 - 32) \div (x - 2)$$

$$\begin{array}{r|rrrrr} 2 & 1 & 0 & 0 & 0 & -32 \\ & 2 & 4 & 8 & 16 & 32 \\ \hline & 2 & 4 & 8 & 16 & 0 \\ & x^4 + 2x^3 + 4x^2 + 8x + 16 & \end{array}$$

$$x^4 + 2x^3 + 4x^2 + 8x + 16$$

18. Simplify:

$$\sqrt[4]{\frac{64x^5y^7}{36xy^2}}$$

$$\sqrt[4]{\frac{64}{36}} = \sqrt[4]{\frac{16}{9}} = \frac{2}{\sqrt[4]{9}} = \frac{2\sqrt[4]{9}}{\sqrt[4]{81}} = \frac{2\sqrt[4]{9}}{3}$$

$$\frac{2}{3}|x|y\sqrt[4]{9y}$$

$$\boxed{\frac{2}{3} \times y \cdot \sqrt[4]{9y}}$$

15. Divide:

$$\frac{\left(\frac{1}{x-4} - \frac{1}{x+4}\right)}{\left(\frac{1}{x-4} + \frac{1}{x+4}\right)}$$

$$\frac{\frac{x+4-x+4}{(x-4)(x+4)}}{\frac{x+4+x-4}{(x-4)(x+4)}} = \frac{8}{2x} = \boxed{\frac{4}{x}}$$

$$\frac{4}{x}$$

17. Divide :

$$(64y^3 - 8) \div (4y - 2)$$

$$\begin{array}{r|rr} 4y-2 & 16y^2 + 8y + 4 \\ \hline & 64y^3 & -8 \\ & 64y^3 - 32y^2 & \\ \hline & 32y^2 & 0 \\ & 32y^2 - 16y & \\ \hline & 16y & -8 \\ & 16y & -8 \\ \hline & 0 & 0 \end{array}$$

19. Complete the three missing boxes

$$\sqrt[3]{\frac{81x^8y^{-3}}{z^2}} = \frac{3 \cdot \boxed{X}}{\boxed{Y} \cdot z} \cdot \sqrt[3]{\boxed{Z}x^2z}$$

Just match two sides.

$$\frac{3x^2}{yz} \sqrt[3]{3x^2z}$$

20. Simplify:

$$2\sqrt{32} - \sqrt{50} + \sqrt{162}$$

$$\begin{aligned} & 2\sqrt{16}\sqrt{2} - \sqrt{25}\sqrt{2} + \sqrt{81}\sqrt{2} \\ & = \sqrt{2}(8 - 5 + 9) = \boxed{12\sqrt{2}} \\ & 12\sqrt{2} \end{aligned}$$

21. Simplify:

$$\sqrt[3]{24} - \sqrt[3]{81}$$

$$\begin{aligned} & \sqrt[3]{3} \cdot \sqrt[3]{8} - \sqrt[3]{27} \cdot \sqrt[3]{3} = \\ & = \sqrt[3]{3} \cdot (2 - 3) = \boxed{-\sqrt[3]{3}} \\ & -\sqrt[3]{3} \end{aligned}$$

22. Simplify (rationalize denominator)

$$\frac{\sqrt{3} + 5}{7 + \sqrt{3}}$$

$$\begin{aligned} & \frac{(\sqrt{3} + 5)(7 - \sqrt{3})}{(7 + \sqrt{3})(7 - \sqrt{3})} = \frac{2\sqrt{3} + 35 - 3}{49 - 3} = \\ & = \frac{2\sqrt{3} + 32}{46} = \boxed{\frac{\sqrt{3} + 16}{23}} \\ & \frac{\sqrt{3} + 16}{23} \end{aligned}$$

23. Simplify (rationalize denominator)

$$\frac{4 - 2i}{4 + 2i}$$

$$\begin{aligned} & \frac{(4 - 2i)(4 + 2i)}{(4 + 2i)(4 - 2i)} = \frac{16 - 16i - 4}{16 + 4} \\ & = \frac{12 - 16i}{20} = \boxed{\frac{3}{5} - \frac{4}{5}i} \end{aligned}$$

24. Simplify

$$(\sqrt{-9} + \sqrt{9}) \cdot (\sqrt{4} + \sqrt{-4})$$

$$\begin{aligned} & (3i + 3)(2 + 2i) = \\ & = 12i + 6 + 6i^2 = \boxed{12i} \\ & 12i \end{aligned}$$

25. Simplify

$$2i \cdot (\sqrt{-9} + \sqrt{9}) + i \cdot (\sqrt{4} + \sqrt{-4})$$

$$\begin{aligned} & i(2 \cdot (3i + 3) + (2 + 2i)) = \\ & = i(8 + 8i) = \boxed{-8 + 8i} \\ & -8 + 8i \end{aligned}$$

26. Solve and check

$$\begin{aligned} & x - 5 = \sqrt{x + 7} \\ & (x - 5)^2 = (\sqrt{x + 7})^2 \\ & x^2 - 10x + 25 = x + 7 \\ & x^2 - 11x + 18 = 0 \\ & x = 9 \end{aligned}$$

$\boxed{x = -9}$ or $x = 12$

Doesn't
check
works

27. Solve and check

$$\sqrt{x + 7} + 8 = x + 3$$

exactly the same!

$$x = 9$$

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28. Solve:

$$x^2 - 81 = 0$$

$$\boxed{x = \pm 9}$$

$$x = +9 \text{ or } x = -9$$

29. Solve :

$$x^2 - 81x = 0$$

$$\begin{aligned} x(x-81) &= 0 \\ \boxed{x=0 \text{ or } x=81} \end{aligned}$$

$$x = 0 \text{ or } x = 81$$

30. Solve

$$-x^2 + 4x - 3 = 0$$

$$x^2 - 4x + 3 = 0$$

$$\frac{4 \pm \sqrt{16-12}}{2} = \frac{4 \pm 2}{2} = 2 \pm 1 \rightarrow 1$$

$$\begin{array}{|c|} \hline \cancel{\frac{\sqrt{3+16}}{23}} & \boxed{x=3} \\ \hline \text{or} & \\ \hline y=1 & \end{array}$$

31. Solve

$$\frac{1}{2}y^2 - 3y + 9 = 0$$

$$y^2 - 6y + 18 = 0$$

$$\frac{6 \pm \sqrt{36-72}}{2} = \frac{6 \pm \sqrt{-36}}{2} = \boxed{3 \pm 3i}$$

$$3 \pm 3i$$

32. Solve

$$x^2 - 4x + 1 = 0$$

$$\frac{4 \pm \sqrt{16-4}}{2} = \frac{4 \pm 2\sqrt{3}}{2} = \boxed{2 \pm \sqrt{3}}$$

$$2 \pm \sqrt{3}$$

33. Solve

$$x^2 + 81 = 0$$

$$x^2 = -81$$

$$\boxed{x = \pm 9i}$$

$$x = 9i$$

34. Find three consecutive integers such that the square of the first plus the product of the other two is 46.

$$x, x+1, x+2.$$

$$x^2 + (x+1)(x+2) = 46$$

$$x^2 + x^2 + 3x + 2 = 46$$

$$2x^2 + 3x + 2 = 46$$

$$4,5,6$$

$$2x^2 + 3x - 44 = 0$$

$$\frac{-3 \pm \sqrt{9+352}}{4} = \frac{-3 \pm 19}{4} =$$

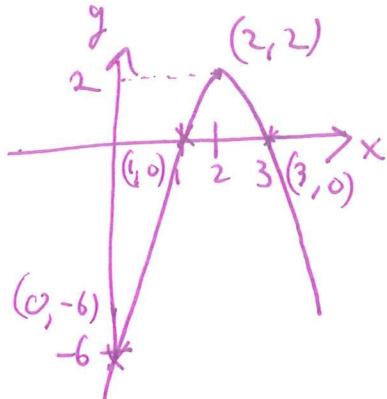
$$\boxed{4, 5, 6}$$

$$= \boxed{4} \times$$

Graph the following functions. Indicate (if relevant) x-intercepts, y-intercepts, vertex, and any other significant points.

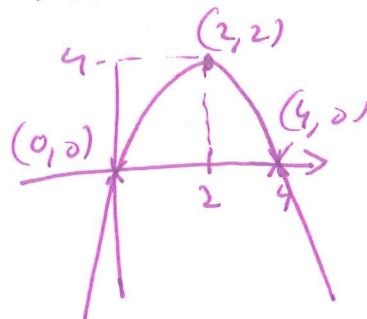
35.

$$f(x) = 2 \cdot (1 - x) \cdot (x - 3)$$



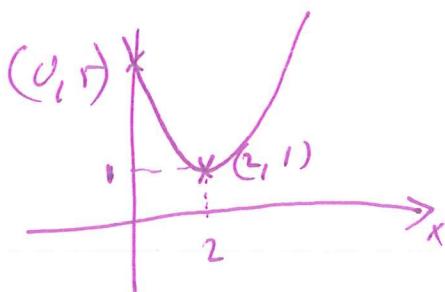
36.

$$f(x) = 4x - x^2$$



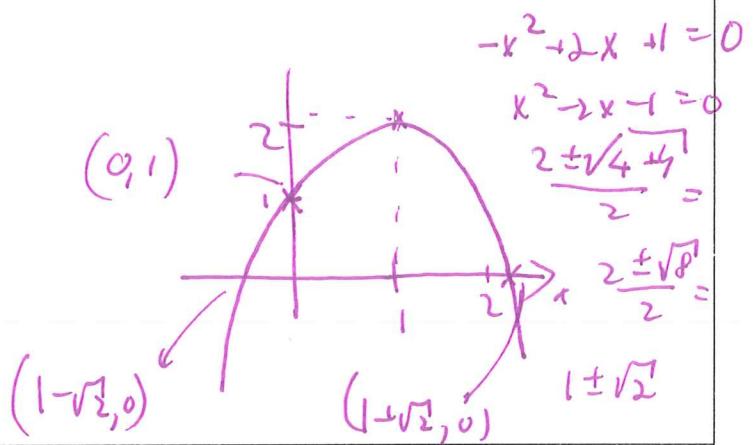
37.

$$f(x) = x^2 - 4x + 5$$



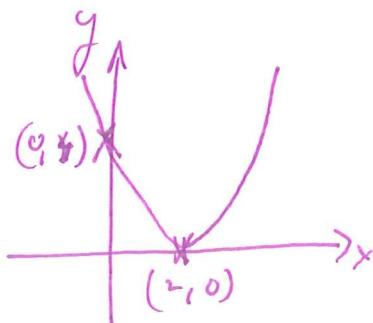
38.

$$f(x) = -(x - 1)^2 + 2$$



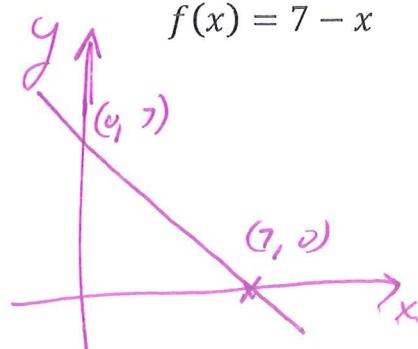
39.

$$f(x) = x^2 - 4x + 4$$



40.

$$f(x) = 7 - x$$



41. Graph the following function

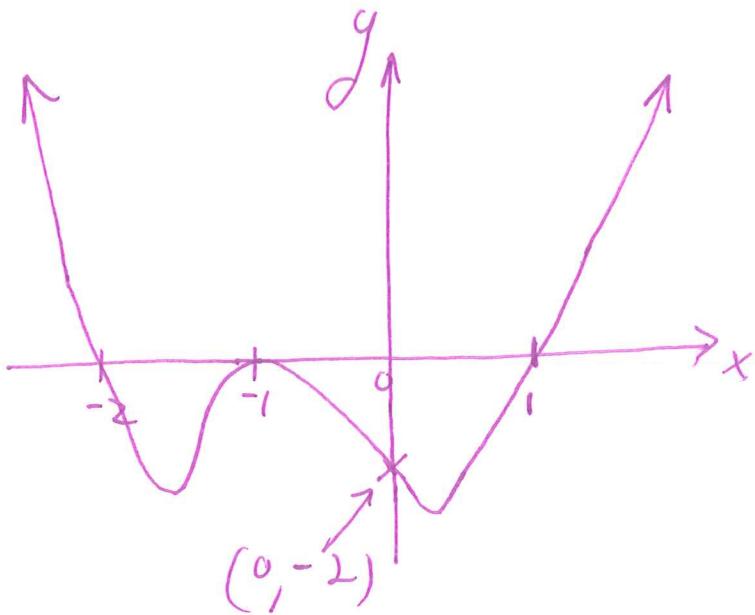
$$f(x) = x^6 + 3x^5 + 2x^4 - x^2 - 3x - 2$$

Hint: The function has roots at -2, 1, -1, and i.

$$(x-(-2))(x-1)(x-(-1))(x-i)(x-(-i)) = (x+2)(x-1)$$

$$f(x) = \underbrace{(x+1)^2}_{\text{Leading coeff: +}}(x-1)(x+2)(x^2+1)$$

degree: 6 $\uparrow \uparrow$

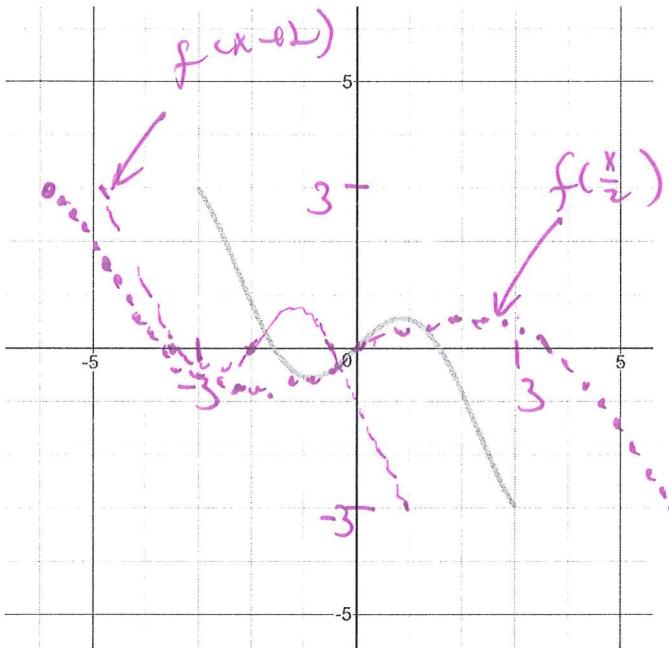


$$(x+1)^2(x-1)(x+2)(x^2+1)$$

42. The sum of two even numbers is 16. Find the numbers such that their product is maximum.

$$\begin{array}{l} \underbrace{2x + 2y = 16}_{\text{even even}} \Rightarrow x + y = 8 \\ P = xy = 4x(8-x) \\ = 4[-x^2 + 8x] \\ b = \frac{-b}{2a} = \frac{-8}{-2} = 4 \\ \Rightarrow \boxed{x = 8 \Rightarrow y = 8} \end{array}$$

43. Given the function $f(x)$:



Find Range and Domain: Domain: $[-3, 3]$ Range: $[-3, 3]$.

Is the function Even/Odd? Odd: $f(x) = -f(-x)$.

Graph $f(x + 2)$. Range and Domain: Domain $[-5, 1]$, Range $[-3, 3]$.

Graph $f\left(\frac{x}{2}\right)$. Range and Domain: $[-6, 6]$ by $[-3, 3]$

44. Solve for x:

a. $x = \log_2 64$
 $x = 6$

$$\boxed{x = 6}$$

b. $2 = \log_7 x$
 $x = 49$

$$\boxed{x = 49}$$

c. $2^{x+2} = 32$
 $x = 3$

$$2^{x+2} = 2^5$$

$$\boxed{x = 3}$$

46. Calculate the following.

a. $\log 4 + \log 250$
 $\log(1000) = 3$

$$\boxed{3}$$

b. $\log_2 3 - \log_2 48$
 $\log_2 \left(\frac{1}{16}\right) = -4$

$$\boxed{-4}$$

c. $\log(10000) - \frac{\log_4 27}{\log_4 3}$
 $4 + \log_3 27 = 7$

$$\boxed{1}$$

$$\boxed{1}$$

48. Determine if each of the below is geometric, arithmetic, or neither

a. $1, 4, 9, 16, 25, 36, \dots$ neither

b. $\frac{1}{2}, \frac{3}{5}, \frac{5}{8}, \frac{8}{11}, \dots$ neither

c. $\frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{7}{2}, \dots$ Arithmetic
 $d = 1$

45. Solve for x:

a. $x^2 = \log_2 16$
 $x = \pm 2$

$$x^2 = 4$$

$$\boxed{|x| = \pm 2}$$

b. $2 = \log_7 (x^2)$
 $x = \pm 7$

$$\boxed{|x| = \pm 7}$$

c. $2^{(x^2)} = 64$
 $x = \pm 3$

$$2^{x^2} = 2^6$$

$$\boxed{|x| = \pm \sqrt{6}}$$

47. Give the value of the following functions.

a. $\cos(30^\circ)$

$$\frac{\sqrt{3}}{2}$$

$$\boxed{\frac{\sqrt{3}}{2}}$$

b. $\sin(30^\circ)$

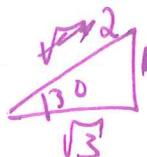
$$0.5$$

$$\boxed{\frac{1}{2}}$$

c. $\tan(30^\circ)$

$$\frac{\sqrt{3}}{3}$$

$$\boxed{\frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}}$$



49. Calculate the sum:

$$\sum_{n=0}^{101} (n - 50) = ?$$

$$\frac{(-50 + 51) \cdot 102}{2} = 51$$

$$\frac{(-50 + 51)}{2} \cdot 102 = \boxed{51}$$

50. Given the functions

$$f(x) = 2x^2 - 1 \quad \text{and} \\ g(x) = x^2 - 3$$

a. Find $f(g(x))$

$$2(x^2 - 3)^2 - 1 = [2x^4 - 12x^2 + 17]$$

b. Find $g(f(x))$

$$(2x^2 - 1)^2 - 3 = [4x^4 - 4x^2 + 1 - 3] = [4x^4 - 4x^2 - 2]$$

c. Find $g(x) + f(x)$

$$2x^2 - 1 + x^2 - 3 = [3x^2 - 4]$$

52. Find the equation of the line perpendicular to the line

$$y = 5 - 2x$$

and that includes through the point $(1, 0)$.

What is the intersection point of these two lines.

$$y = 5 - 2x \Rightarrow m = -2$$

$$y = \frac{1}{2}x + b \quad \leftarrow m_{\perp} = \frac{1}{2}$$

$$(1, 0) \Rightarrow y = \frac{1}{2}x - \frac{1}{2} \quad \checkmark$$

51. Find the inverse of $f(x)$ using Table and algebraic method, and plot both:

$$f(x) = 1 - \sqrt{x - 2}$$

Remember to indicate range and domain of each function.

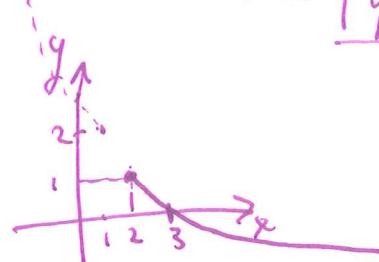
$$\text{Domain } f(x) = [2, \infty)$$

$$\text{Range } f(x) = (-\infty, 1]$$

$\xrightarrow{\text{inverse}}$

$$\text{inverse: } [y = (x - 1)^2 + 2]$$

$$x \leq 1.$$



Word problems: See set II

==== End of practice questions (There IS part II: Word problems and miscellaneous).