

Name: _____

Date: _____

Class/Home worksheet: Alg2H
Factoring (book chapter 5, page 519 and beyond)

Factoring is the reverse of multiplying.

Factoring an expression means to write it as an equivalent expression that is a product.

Common factor:

$$3x^2 + 12 =$$

$$3 \cdot x^2 + 3 \cdot 4 =$$

$$3 \cdot (x^2 + 4)$$

Common factor:

$$7x^3 + 14x^2 =$$

$$7x^2(x + 2)$$

Common factor:

$$5x^3 - 20x^3 =$$

$$5x^3(1 - 4)$$

Common factor:

$$12x^2y - 20x^3y =$$

$$4x^2y(3 - 5x)$$

Common factor:

$$10a^4 + 15a^2 - 25a =$$

$$\boxed{5a(2a^3 + 3a - 5)}$$

$$5a(2a^3 + 2a - 5a - 5)$$

$$5a(\text{stays as is!})$$

Common factor:

$$9x^3y^2 - 6x^2y^3 + 3x^3y^3 =$$

$$3x^2y^2(3x - 2y + xy)$$

Take a common factor if possible.
It will simplify things!

Difference of Squares (P. 221)

$$A^2 - B^2 = (A + B) \cdot (A - B)$$

Factor:

$$x^2 - 25 =$$

$$(x+5)(x-5)$$

Factor:

$$9x^2 - 16y^2 =$$

$$(3x+4y)(3x-4y)$$

Factor:

$$\frac{1}{25} - x^2 =$$

$$\left(\frac{1}{5} - x\right)\left(\frac{1}{5} + x\right)$$

Factor (challenge):

$$x^{16} - 1 =$$

$$\begin{aligned} (x^4 - 1)(x^4 + 1) &= \\ = (x^2 - 1)(x^2 + 1)(x^4 + 1) &= (x+1)(x-1)(x^2+1) \cdot (x^4+1) \end{aligned}$$

Perfect Squares (P. 220)

$$A^2 + 2AB + B^2 = (A + B)^2$$

$$A^2 - 2AB + B^2 = (A - B)^2$$

Factor:

$$x^2 + 10x + 25 =$$

$$(x+5)^2$$

Factor:

$$x^2 - 14x + 49 =$$

$$(x-7)^2$$

Factor (hint: rearrange):

$$16y^2 + 49 + 56y =$$

$$\begin{aligned} 16y^2 + 56y + 49 &= \\ = (4y+7)^2 \end{aligned}$$

Factor:

$$72xy + 16x^2 + 81y^2 =$$

$$\begin{aligned} 16x^2 + 72xy + 81y^2 &= \\ = (4x+9y)^2 \end{aligned}$$

Factoring trinomials MATH style

(The common method in Kehillah school!)

Assume a trinomial of the form



$$aX^2 + bX + c$$

Create the following table following the directions below it:

| M | A | T | H |
|-----------------------|-------------|---|---|
| $a \cdot c \cdot X^2$ | $b \cdot X$ | Try the various factors of $a \cdot c$ that sum up to b | ☺ |

1. Put under M (Multiply) the product $a \cdot c \cdot X^2$
2. Put under A (Add) the value of $b \cdot X$
3. Under T (Tries), put the various factor-pairs of the result in M, and try to see if their sum adds up to A.
4. When you find an appropriate pair, mark a smiley face in H (Happy) !
5. Rewrite the trinomial, by writing the middle term as the sum of two terms, and factor by grouping appropriate terms.

Examples:

I. $3x^2 + 8x + 4$

| M | A | T | H |
|---------|------|------------------|---|
| $12x^2$ | $8x$ | $3, 4$ $6, 2$ | ✓ |

$$\begin{aligned}
 &3x^2 + 6x + 2x + 4 \\
 &= 3x(x+2) + 2(x+2) = \boxed{(3x+2)(x+2)}
 \end{aligned}$$

II. $2x^2 + x - 15$

| M | A | T | H |
|----------|-------------|----------------------|---|
| $-30x^2$ | $1 \cdot x$ | $-6, 5$ $6x - 5x$ | ✓ |

$$2x^2 + 6x - 5x - 15 = 2x(x+3) - 5(x+3) = (2x-5)(x+3)$$

If I take: $2x^2 - 5x + 6x - 15 = x(2x-5) + 3(2x-5) = (x+3)(2x-5) ✓$

III. $x^2 - 2x - 24$

| M | A | T | H |
|----------|-------|--------------------------------|---|
| $-24x^2$ | $-2x$ | $-12, 2$ $6, -4$ $-6, 4$ | ✓ |

$$x^2 - 6x + 4x - 24 = x(x-6) + 4(x-6) = (x+4)(x-6)$$

Let's try in the case of binomial (though we know the answer already!)

IV. $4x^2 - 9 = 4x^2 + 0x - 9$

| M | A | T | H |
|----------|---|---------|---|
| $-36x^2$ | 0 | $6, -6$ | ✓ |

$$4x^2 + 6x - 6x - 9 = 2x(2x+3) - 3(2x+3) = (2x-3)(2x+3)$$

V. $-2x^2 - x + 6$

| M | A | T | H |
|----------|------|--------------------|---|
| $-12x^2$ | $-x$ | $-6, 2$ $-4, 3$ | ✓ |

$$-2x^2 - 4x + 3x + 6 = -2x(x+2) + 3(x+2) = (3-2x)(x+2)$$

From the book, Page 223

(30) $12a^2 + 36a + 27 =$

$$3(4a^2 + 12a + 9) =$$

$$3(2a+3)^2$$

(38) $9x^2 - 25 =$

$$(3x+5)(3x-5)$$

(46) (tricky: Don't stop in the middle)

$4xy^4 - 4xz^4 =$

$$4x(y^4 - z^4) =$$

$$4x(y^2 - z^2)(y^2 + z^2) =$$

$$4x(y+z)(y-z)(y^2 + z^2)$$

Factor:

$x^2 + 9x + 20 =$

| M | A | T |
|---------|------|--------|
| $20x^2$ | $9x$ | $4, 5$ |

$$x^2 + 4x + 5x + 20 =$$

$$= x(x+4) + 5(x+4) = (x+5)(x+4)$$

Factor:

$4x^2 - 3 + 4x = 4x^2 + 4x - 3$

| M | A | T |
|----------|------|---------|
| $-12x^2$ | $4x$ | $-6, 2$ |

$$= 4x^2 + 2x - 6x - 3 =$$

$$= 2x(2x+1) - 3(2x+1) =$$

$$(2x-3)(2x+1)$$

Factor:

$6x^2 + 17x + 7 =$

| M | A | T |
|---------|-------|-------------------|
| $42x^2$ | $17x$ | $7, 6$ $14, 3$ |

$$6x^2 + 3x + 14x + 7 =$$

$$3x(2x+1) + 7(2x+1) =$$

$$(3x+7)(2x+1)$$

Two more items for factoring: Grouping and Cubes

checking: $6x^2 + 14x + 3x + 7 =$

$$= 2x(3x+7) + 1(3x+7) = (2x+1)(3x+7)$$